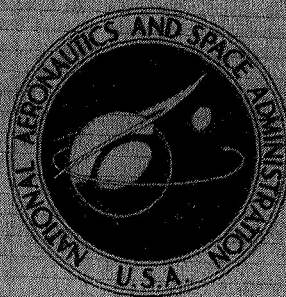


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## HELICAL DUCT GEOMETRY ROUTINE FOR THE SHIELDING COMPUTER PROGRAM "FASTER"

*by Thomas M. Jordan and Millard L. Wobl*

*Lewis Research Center*

*Cleveland, Ohio*

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NATIONAL AERONAUTICS AND SPACE ADMINISTRATION

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## ABSTRACT

A method for tracking neutrons through a slab penetrated by a helical voided duct is presented and verified. FORTRAN listings of computer subroutines that perform the numerical analysis are included; these subroutines are designed to be used with FASTER, a high-efficiency Monte Carlo code. Neutron number spectra were calculated at several points in and near the emergent end of a duct through a 20- and a 100-centimeter thick water slab having a point source at the center of the inlet.

# HELICAL DUCT GEOMETRY ROUTINE FOR THE SHIELDING COMPUTER PROGRAM "FASTER"

by Thomas M. Jordan\* and Millard L. Wohl

Lewis Research Center

## SUMMARY

A method for tracking neutrons through slabs penetrated by helical voided ducts is presented and verified by means of the FASTER computer code. A point fission source is located at the center of the entrant mouth of the duct. Neutron number spectra computed at point detectors in and near the emergent mouth of the duct are compared with similar results computed by the FASTER code and the O5R code using cylindrical geometry to describe the duct. The helical duct is given a very large pitch to simulate a cylindrical duct within the slabs considered. The comparison of number spectra is almost exact, verifying the techniques developed herein. FORTRAN listings of computer subroutines that perform the numerical analysis are included; these subroutines are designed to be used in conjunction with FASTER, a high-efficiency Monte Carlo code.

## INTRODUCTION

A useful reactor coolant flow passage geometry is that of a helicoid, or a helical tubular duct. This duct configuration has the dual advantage of reducing radiation streaming through a shield and permitting low coolant pressure drop.

In order to track neutrons and gamma rays through such a complex geometric configuration, subroutines are written to be used with the FASTER code. Sample problems (ref. 1), previously run with cylindrical ducts with the FASTER and O5R codes, were solved using a helical duct; this was done by assigning a pitch of  $10^5$  centimeters to a helicoid penetrating a 20- and a 100-centimeter-thick water slab. Thus, the important within-slab region of the helicoid is essentially cylindrical.

Agreement was obtained for the neutron number spectrum at several point detectors in and near the emergent mouth of a duct having a point fission neutron source at the

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\*ART Research Corporation, Los Angeles, California.



center of one end of the duct. This agreement verified the helical duct geometry handling subroutines.

## ANALYSIS

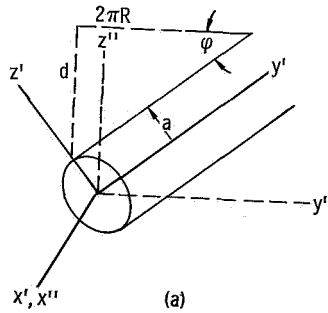
The equation of the helicoid is developed by using the fact that the intersection of the surface and a cutting plane normal to the centerline of the helicoid is circular. The parametric equations of the duct centerline are

$$x = R \cos \omega z \quad (1a)$$

$$y = R \sin \omega z \quad (1b)$$

where  $\omega = 2\pi/d$ ,  $d$  is the pitch of the helical centerline, and  $R$  is the perpendicular distance from the axis of the cylinder around which the helicoid is wound to the helical centerline.

A point (the origin of the double primed coordinate system is sketch (a)) is first fixed at an arbitrary azimuthal angle  $\theta$ . Solving for the equivalent  $z$ -coordinate gives  $z_0 = \theta/\omega$ . A coordinate system is centered at this point so that its  $y'$ -axis is tangent to the helical centerline and its  $x'$ -axis is along the cylindrical radius vector as in sketch (a):



In the primed coordinate system, the intersection of the unwound helical duct with the cutting plane has the following equation:

$$x'^2 + z'^2 = a^2 \quad (2)$$

where  $a$  is the inner radius of the duct. Performing a rotation  $\phi$  about the  $x'$ -axis, the appropriate transformation equations become

$$x' = x'' \quad (3a)$$

$$y' = y'' \cos \varphi + z'' \sin \varphi \quad (3b)$$

$$z' = -y'' \sin \varphi + z'' \cos \varphi \quad (3c)$$

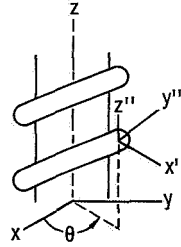
$$\sin \varphi = \frac{d}{[d^2 + (2\pi R)^2]^{1/2}} = \frac{1}{(1 + \omega^2 R^2)^{1/2}} \quad (3d)$$

$$\cos \varphi = \frac{2\pi R}{[d^2 + (2\pi R)^2]^{1/2}} = \frac{\omega R}{(1 + \omega^2 R^2)^{1/2}} \quad (3e)$$

or

$$x''^2 + (-y'' \sin \varphi + z'' \cos \varphi)^2 = a^2 \quad (4)$$

The double primed coordinate system must also be translated and rotated as indicated in sketch (b) and equations (5).



(b)

$$x'' = x \cos \theta + y \sin \theta - R \quad (5a)$$

$$y'' = -x \sin \theta + y \cos \theta \quad (5b)$$

$$z'' = z - z_0 \quad (5c)$$

so that

$$(x \cos \theta + y \sin \theta - R)^2 + [(-x \sin \theta + y \cos \theta) \sin \varphi + (z - z_0) \cos \varphi]^2 = a^2 \quad (6)$$

To put everything in terms of the  $x$ ,  $y$ , and  $z$  coordinates, the following relations are used:

$$\left. \begin{aligned} \theta &= \tan^{-1}\left(\frac{y}{x}\right) & \sin \theta &= \frac{y}{(x^2 + y^2)^{1/2}} \\ z_o &= \frac{1}{\omega} \tan^{-1}\left(\frac{y}{x}\right) & \cos \theta &= \frac{x}{(x^2 + y^2)^{1/2}} \end{aligned} \right\} \quad (7)$$

The resulting equation is

$$\left[ x \frac{x}{(x^2 + y^2)^{1/2}} + y \frac{y}{(x^2 + y^2)^{1/2}} - R \right]^2 + \left\{ \frac{-xy}{(x^2 + y^2)^{1/2}} + \frac{xy}{(x^2 + y^2)^{1/2}} \right\} \sin \varphi + \left[ z - \frac{1}{\omega} \tan^{-1}\left(\frac{y}{x}\right) \right] \frac{\omega R}{(1 + \omega^2 R^2)^{1/2}} \right\}^2 = a^2 \quad (8a)$$

or

$$\left[ (x^2 + y^2)^{1/2} - R \right]^2 + \frac{R^2}{1 + \omega^2 R^2} \left[ \tan^{-1}\left(\frac{y}{x}\right) - \omega z \right]^2 = a^2 \quad (8b)$$

It should be noted that the arctangent function subroutine will return only the principal value. Therefore, in the actual computations the quantity  $\left[ \tan^{-1}(y/x) - \omega z \right]$  will be treated as modulo  $\pi$ .

Equation (8b) is generalized to the following form:

$$\varphi(\vec{r}) = \left\{ \left[ (x_j - x_j^o)^2 + (x_k - x_k^o)^2 \right]^{1/2} - R \right\}^2 + \frac{R^2}{1 + \omega^2 R^2} \left[ \tan^{-1}\left(\frac{x_k - x_k^o}{x_j - x_j^o}\right) - \omega (x_i - x_i^o) \right]^2 - a^2 \quad (9)$$

where  $\varphi(\vec{r})$  is the helicoid surface function and has the following values:

$$\begin{aligned}\varphi(\vec{r}) &= 0 \quad \text{on the helicoid surface} \\ &> 0 \quad \text{outside the surface} \\ &< 0 \quad \text{within the surface}\end{aligned}$$

and where  $(i, j, k) = (1, 2, 3), (2, 3, 1),$  or  $(3, 1, 2)$ ;  $x_1, x_2, x_3 = x, y, z$ ; and  $x_i^0, x_j^0, x_k^0$  are coordinates of the origin of a translated coordinate system.

Thus, the following data are normally supplied to describe the helical duct:  
 $i, x_i^0, x_j^0, x_k^0, d, R, a.$

## VALUES OF THE SURFACE FUNCTION

The computer subroutine has been written to evaluate the surface function at the point  $\vec{r} = \vec{r}_0 + s\vec{\Omega}$  where  $\vec{r}_0$ ,  $\vec{\Omega}$ , and  $S$  are arguments supplied to the subroutine. Let

$$r_0 = (x^*, y^*, z^*) = (x_1^*, x_2^*, x_3^*)$$

$$\vec{\Omega} = (\alpha, \beta, \gamma) = (C_1, C_2, C_3)$$

Then

$$r = (x, y, z) = (x_1, x_2, x_3) = (x_1^* + C_1 S, x_2^* + C_2 S, x_3^* + C_3 S) \quad (10)$$

The value  $\varphi(\vec{r})$  of the surface function is obtained by substituting  $\vec{r}$  from equation (10) into equation (9).

## NORMAL VECTOR

The components of the normal vector  $n$  are

$$\vec{n} = (n_1, n_2, n_3) \quad (11)$$



and are calculated as

$$n_l = \frac{\frac{\partial \varphi}{\partial x_l}}{\sum_{m=1}^3 \left( \frac{\partial \varphi}{\partial x_m} \right)^2} \quad (12)$$

and

$$l = 1, 2, 3$$

The partial derivatives are calculated as

$$\frac{\partial \varphi}{\partial x_i} = -2\omega h v \quad (13a)$$

$$\frac{\partial \varphi}{\partial x_j} = 2 \left( \frac{\hat{x}_j u}{\zeta} - \frac{h v \hat{x}_k}{\zeta^2} \right) \quad (13b)$$

$$\frac{\partial \varphi}{\partial x_k} = 2 \left( \frac{\hat{x}_k u}{\zeta} + \frac{h v \hat{x}_j}{\zeta^2} \right) \quad (13c)$$

where  $(\hat{x}_i, \hat{x}_j, \hat{x}_k) = \left[ (x_i - x_i^0), (x_j - x_j^0), (x_k - x_k^0) \right]$  and

$$\zeta = \left[ (x_j - x_j^0)^2 + (x_k - x_k^0)^2 \right]^{1/2} \quad (14a)$$

$$u = \zeta - R \quad (14b)$$

$$v = \tan^{-1} \left( \frac{x_k - x_k^0}{x_j - x_j^0} \right) - \omega (x_i - x_i^0) \quad (14c)$$

$$h = \frac{R^2}{1 + \omega^2 R^2} \quad (14d)$$

## Intersections With Straight Line

The intersection of a straight line with the helicoid is calculated by an iterative process. The assumption is made that the surface function is locally quadratic. Then the value of the function can be expressed by a truncated Taylor series as

$$\varphi(\vec{r}') = \varphi(\vec{r} + S\Omega) = \varphi(\vec{r}) + S \frac{\partial \varphi(\vec{r})}{\partial S} + \frac{S^2}{2} \frac{\partial^2 \varphi(\vec{r})}{\partial S^2} \quad (15)$$

where  $\varphi(\vec{r})$  is determined from equation (9), and the coefficient  $\partial \varphi(\vec{r})/\partial S$  is calculated from

$$\frac{\partial \varphi(\vec{r})}{\partial S} = \sum_{m=1}^3 C_m \frac{\partial \varphi(\vec{r})}{\partial x_m} \quad (16)$$

using equation (13) to compute the partial derivatives.

The final coefficient is given by

$$\frac{\partial^2 \varphi(\vec{r})}{\partial S^2} = \sum_{l=1}^3 \sum_{m=1}^3 C_l C_m \frac{\partial^2 \varphi(\vec{r})}{\partial x_l \partial x_m} \quad (17)$$

where

$$\frac{\partial^2 \varphi(\vec{r})}{\partial x_i^2} = 2h\omega^2 \quad (18a)$$

$$\frac{\partial^2 \varphi(\vec{r})}{\partial x_j^2} = 2 \left[ \frac{\hat{u}x_k^2}{\zeta^3} + \frac{\hat{x}_j^2}{\zeta^2} + h \left( \frac{2v\hat{x}_j\hat{x}_k}{\zeta^4} + \frac{\hat{x}_k^2}{\zeta^4} \right) \right] \quad (18b)$$

$$\frac{\partial^2 \varphi(\vec{r})}{\partial x_k^2} = 2 \left[ \frac{\hat{u}x_j^2}{\zeta^3} + \frac{\hat{x}_k^2}{\zeta^2} + h \left( \frac{-2v\hat{x}_j\hat{x}_k}{\zeta^4} + \frac{\hat{x}_j^2}{\zeta^4} \right) \right] \quad (18c)$$

$$\frac{\partial^2 \varphi(\vec{r})}{\partial \hat{x}_i \partial \hat{x}_j} = \frac{2h\omega \hat{x}_k}{\zeta^2} \quad (18d)$$

$$\frac{\partial^2 \varphi(\vec{r})}{\partial \hat{x}_j \partial \hat{x}_k} = 2 \left\{ \frac{-u \hat{x}_j \hat{x}_k}{\zeta^3} + \frac{\hat{x}_j \hat{x}_k}{\zeta^2} + h \left[ \frac{v (\hat{x}_k^2 - \hat{x}_j^2)}{\zeta^4} - \frac{\hat{x}_j \hat{x}_k}{\zeta^4} \right] \right\} \quad (18e)$$

$$\frac{\partial^2 \varphi(\vec{r})}{\partial \hat{x}_k \partial \hat{x}_i} = \frac{-2h\omega \hat{x}_j}{\zeta^2} \quad (18f)$$

The net result is a quadratic equation for the distance  $S$  to the surface since the surface function  $\varphi(\vec{r})$  must be zero at the intersection

$$\varphi(\vec{r}') = \varphi(\vec{r}) + S \frac{\partial \varphi(\vec{r})}{\partial S} + \frac{S^2}{2} \frac{\partial^2 \varphi(\vec{r})}{\partial S^2} = 0 \quad (19)$$

Let

$$A = \frac{\partial^2 \varphi(\vec{r})}{\partial S^2} \quad (20a)$$

$$B = \frac{\partial \varphi(\vec{r})}{\partial S} \quad (20b)$$

$$C = 2\varphi(\vec{r}) \quad (20c)$$

Then

$$AS^2 + 2BS + C = 0 \quad (21a)$$

or

$$S = \frac{-B \pm \delta \sqrt{B^2 - AC}}{A} \quad (21b)$$

The sign of the square root is determined by the ambiguity index  $\delta$  (of eq. (21b)) with respect to the region in which the ray tracing is performed. The ambiguity index

is defined as

$$\delta = \frac{-\varphi(\vec{r}_g)}{\varphi(\vec{r}_g)} \quad (22)$$

where  $\vec{r}_g$  is any point in the region.

Equation (21) is not used when  $|AC/B^2| < 10^{-4}$ . A one-term expansion is then used for the square root so that

$$S = -\frac{B}{A} \left( 1 - \delta \frac{B}{|B|} \right) = \frac{1}{2} \frac{C\delta}{|B|} \quad (23)$$

This procedure eliminated convergence problems caused by underflow in the vicinity of the intersection.

The distance  $S$  to the intersection is used to compute a new reference point  $\vec{r}$  and the entire procedure is then repeated until the change in  $S$  is less than  $10^{-5}$  of the value already obtained. In general, only two iterations are needed.

The changes required to incorporate the helical duct in FASTER are shown in the appendix. The input instructions are modified to include the following on card 2-2:

$i, 0, 16, x^0, y^0, z^0, L, R, a$	$i^{\text{th}}$ surface has helix axis parallel to x-axis
$i, 0, 17, y^0, z^0, x^0, L, R, a$	$i^{\text{th}}$ surface has helix axis parallel to y-axis
$i, 0, 18, z^0, x^0, y^0, L, R, a$	$i^{\text{th}}$ surface has helix axis parallel to z-axis

## RESULTS AND DISCUSSION

The duct analysis routine was verified by using it for the 20- and 100-centimeter-thick water slab cylindrical duct problem previously run as shown in figure 1 (ref. 1). Neutron number spectra essentially coincided with previously calculated spectra (O5R and FASTER with cylindrical duct geometry) as seen in figure 2. The cylindrical duct was simulated with the helicoid geometry subroutines by making  $L$ , the pitch, equal to  $10^5$  centimeters. Neutron number spectra at each detector point were calculated using 1000 histories. Computer time was 20 minutes per detector point, approximately double



that required for solution of the same problem using the cylindrical geometry routine, as expected because of the more complex geometric description of the cylindrical duct.

Lewis Research Center,  
National Aeronautics and Space Administration,  
Cleveland, Ohio, June 2, 1969,  
126-15-01-03-22.

## APPENDIX - LISTING

### Changes to FASTER for Subroutine HELIX

```

C TO INCORPORATE SUBROUTINE HELIX IN FASTER, MAKE THE FOLLOWING CHANGES
C
C SUBROUTINE LOCDUM
C
C INSERT AFTER FAST0151
      IF (MAX.GT.9) CALL HELIX(1,MAX-9,A(1,K),X,X,0,0,U(K))
      IF (MAX.GT.9) GO TO 160
C
C SUBROUTINE GEOMIN
C
C REPLACE FAST0532 BY
      GO TO(232,233,235,260,255,282),NGT
C INSERT AFTER FAST0579
      GO TO 290
      282 DO 284 J=1,6
      284 A(J,I) = AA(J)
      NTP(I) = NEX + 9
C INSERT AFTER FAST0616
      IF (MAX.GT.9) CALL HELIX(1,MAX-9,A(1,K),ADM,ADM,0,0,FST)
      IF (MAX.GT.9) GO TO 335
C INSERT AFTER FAST0619
      335 CONTINUE
C
C SUBROUTINE TRADUM
C
C INSERT AFTER FAST2228
      IF (NTP(K).LE.9) GO TO 198
      IF (M.GT.1) GO TO 192
      SI(1,K) = STT
      SI(2,K) = STT + SP
      CALL HELIX(3,KK*(NTP(K)-9),A(1,K),X,C,SI(1,K),SR)
      IF (SB) 340,330,330
      192 CALL HELIX(1,NTP(K)-9,A(1,K),X,C,STT,FST)
      IF (FLOAT(KK)*FST) 340,340,390
      198 CONTINUE
C
C SUBROUTINE NORDUM
C
C INSERT AFTER FAST2343
      IF (MAX.GT.9) CALL HELIX(2,MAX-9,A(1,I),X,X,0,0,C)
      IF (MAX.GT.9) GO TO 35
C INSERT AFTER FAST2355
      35 CONTINUE

```

FAST0151  
FAST0151

FAST0532

FAST0579  
FAST0579  
FAST0579  
FAST0579

FAST0616  
FAST0616

FAST0619

FAST2228  
FAST2228  
FAST2228  
FAST2228  
FAST2228  
FAST2228  
FAST2228  
FAST2228  
FAST2228

FAST2343  
FAST2343

FAST2355

## Subroutine HELIX Listing

```

C*****
C /JARG/ = 1, HELIX PARALLEL TO X-AXIS (I,J,K)=(1,2,3)=(X,Y,Z)
C /JARG/ = 2, HELIX PARALLEL TO Y-AXIS (I,J,K)=(2,3,1)=(Y,Z,X)
C /JARG/ = 3, HELIX PARALLEL TO Z-AXIS (I,J,K)=(3,1,2)=(Z,X,Y)
C SIGN(JARG) = AMBIGUITY INDEX
C VARG(1) = REFERENCE VALUE OF X(I) AT WHICH THETA = 0.0
C VARG(2) = TRANSLATION OF HELIX AXIS IN X(J) DIRECTION
C VARG(3) = TRANSLATION OF HELIX AXIS IN X(K) DIRECTION
C VARG(4) = PERIOD OF HELIX ALONG X(I) AXIS
C VARG(5) = RADIUS OF GYRATION OF HELIX PERPENDICULAR TO X(I) AXIS
C VARG(6) = RADIUS OF HELIX CROSS SECTION
C WARG(1) = X COORDINATE OF ORIGIN OF RAY
C WARG(2) = Y COORDINATE OF ORIGIN OF RAY
C WARG(3) = Z COORDINATE OF ORIGIN OF RAY
C XARG(1) = DIRECTION COSINE OF RAY WITH RESPECT TO X AXIS
C XARG(2) = DIRECTION COSINE OF RAY WITH RESPECT TO Y AXIS
C XARG(3) = DIRECTION COSINE OF RAY WITH RESPECT TO Z AXIS
C YARG(1) = DISTANCE ALREADY TRAVERSED ALONG RAY
C YARG(2) = MAXIMUM DISTANCE ALONG RAY
C IARG = 1, COMPUTE VALUE OF HELIX      RETURNED IN ZARG(1)
C IARG = 2, COMPUTE NORMAL VECTOR      RETURNED IN ZARG(1),...,ZARG(3)
C IARG = 3, COMPUTE DISTANCE TO HELIX  RETURNED IN ZARG(1)
C*****
      SUBROUTINE HELIX(IARG,JARG,VARG,WARG,XARG,YARG,ZARG)
      DIMENSION VARG(1),WARG(1),XARG(1),YARG(1),ZARG(1)
      DIMENSION XZ(3),X(3),C(3),CN(3)
      DATA      KOUNT,PI,TPI/0.3,1415927,6.2831853/
      DO 100 I=1,3
      C(I)      = XARG(I)
      XZ(I)     = WARG(I) + C(I)*YARG(1)
100  X(I)      = XZ(I)
      NGT      = IARG
      I        = IABS(JARG)
      J        = I + 1 - 3*(I/3)
      K        = J + 1 - 3*(J/3)
      TPL      = TPI/VARG(4)
      GAM      = 1.0/(TPL**2 + 1.0/VARG(5)**2)
110  DXI      = X(I) - VARG(1)
      DXJ      = X(J) - VARG(2)
      DXK      = X(K) - VARG(3)
      USM      = SQRT(DXJ**2 + DXK**2)
      THE      = 0.0
      IF(USM.GT.0.0) THE = ATAN2(DXK,DXJ) - TPL*DXI
      VSM      = THE - TPI*FLOAT(IFIX((THE + PI)/TPI))
      URG      = USM - VARG(5)
      PHI      = URG**2 + GAM*VSM**2 - VARG(6)**2
      IF(NGT.GT.1) GO TO 120
      ZARG(1) = PHI
      GO TO 990
120  CST      = DXJ/USM
      SNT      = DXK/USM
      CN(I)    = -TPL*GAM*VSM
      CN(J)    = URG*CST - GAM*VSM*SNT/USM
      CN(K)    = URG*SNT + GAM*VSM*CST/USM
      DPH      = 0.0
      IF(NGT.GT.2) GO TO 150
      DO 130 I=1,3
130  DPH      = DPH + CN(I)**2
      DPH      = SQRT(DPH)
      DO 140 I=1,3
140  ZARG(I) = CN(I)/DPH
      GO TO 990

```

150 DO 160 L=1,3	HELIX390
160 DPH = DPH + C(L)*CN(L)	HELIX400
CN(I) = GAM*TPL**2	HELIX410
CN(J) = URG*SNT**2/USM+CST**2+GAM*SNT*(2.0*VSM*CST+SNT)/USM**2	HELIX420
CN(K) = URG*CST**2/USM+SNT**2-GAM*CST*(2.0*VSM*SNT-CST)/USM**2	HELIX430
DDP = 0.0	HELIX440
DO 170 L=1,3	HELIX450
170 DDP = DDP + CN(L)*C(L)**2	HELIX460
CN(I) = TPL*GAM*SNT/USM	HELIX470
CN(J) = SNT*CST*(1.0 - URG/USM)	HELIX480
1     + GAM*(VSM*(SNT**2 - CST**2) - SNT*CST)/USM**2	HELIX485
CN(K) = -TPL*GAM*CST/USM	HELIX490
DO 180 L=1,3	HELIX500
M = L + 1 - 3*(L/3)	HELIX510
180 DDP = DDP + 2.0*CN(L)*C(L)*C(M)	HELIX520
IF(NGT.GT.3) GO TO 190	HELIX530
TOT = 0.0	HELIX540
KK = I/JARG	HELIX550
SGN = FLOAT(KK)	HELIX560
STB = 2.0*YARG(2)	HELIX570
190 H = 0.0	HELIX580
NEH = 0	HELIX590
DLS = 0.0	HELIX600
IF(PHI.NE.0.0) GO TO 200	HELIX610
IF(DDP.210,250,210)	HELIX620
200 IF(DDP.NE.0.0) GO TO 210	HELIX630
DLS = -0.5*PHI/DPH	HELIX640
GO TO 250	HELIX650
210 IF(DPH.EQ.0.0) GO TO 220	HELIX660
IF(ABS(DDP*PHI/DPH**2).GT.1.0E-4) GO TO 220	HELIX670
ADP = ABS(DPH)	HELIX680
DLS = ADP*(SGN - DPH/ADP)/DDP - 0.5*SGN*PHI/ADP	HELIX690
GO TO 250	HELIX700
220 DLS = -DPH/DDP	HELIX710
H = DPH**2 - DDP*PHI	HELIX720
IF(H) 230,250,240	HELIX730
230 NEH = 1	HELIX740
GO TO 250	HELIX750
240 DLS = DLS + SGN*SQRT(H)/DDP	HELIX760
250 IF((DLS + TOT).LE.0.0) GO TO 290	HELIX770
TOT = TOT + DLS	HELIX780
IF((NEH.GT.0).AND.(NGT.GT.3)) GO TO 290	HELIX790
IF(NEH.GT.0) GO TO 260	HELIX800
IF(ABS(DLS/TOT).LE.1.0E-5) GO TO 280	HELIX810
IF(NGT.GT.4) GO TO 280	HELIX820
260 DO 270 L=1,3	HELIX830
270 X(L) = XZ(L) + TOT*C(L)	HELIX840
NGT = NGT + 1	HELIX850
GO TO 110	HELIX860
280 STB = TOT	HELIX870
IF(DLS.LE.0.0) STB = STB + AMAX1(-DLS,1.0E-5*TOT)	HELIX880
290 ZARG(1) = STB	HELIX890
KOUNT = KOUNT + 1	HELIX900
IF(KOUNT.LE.100) WRITE(6,2000)NGT,I,J,K,KK,NEH,X,C,DDP,DPH,PHI,	HELIX910
1TOT,DLS,STB	HELIX920
990 RETURN	HELIX930
2000 FORMAT(1X,6I6,1P6E12.4/37X,6E12.4)	HELIX940
END	HELIX950



## REFERENCE

1. Wohl, Millard L.; and Jordan, Thomas M.: Use of "FASTER" Code for Significantly Reducing Ducted Reactor Shield Computation Time. NASA TM X-1828, 1969.

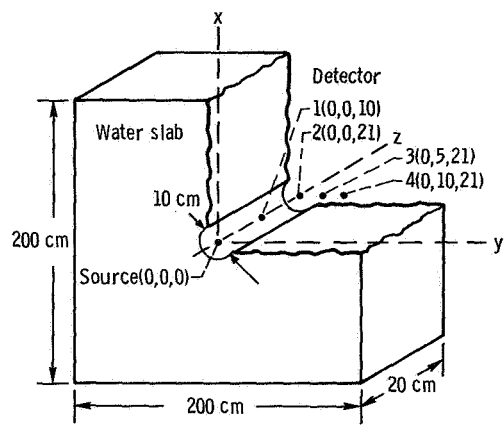


Figure 1. - Problem configuration.

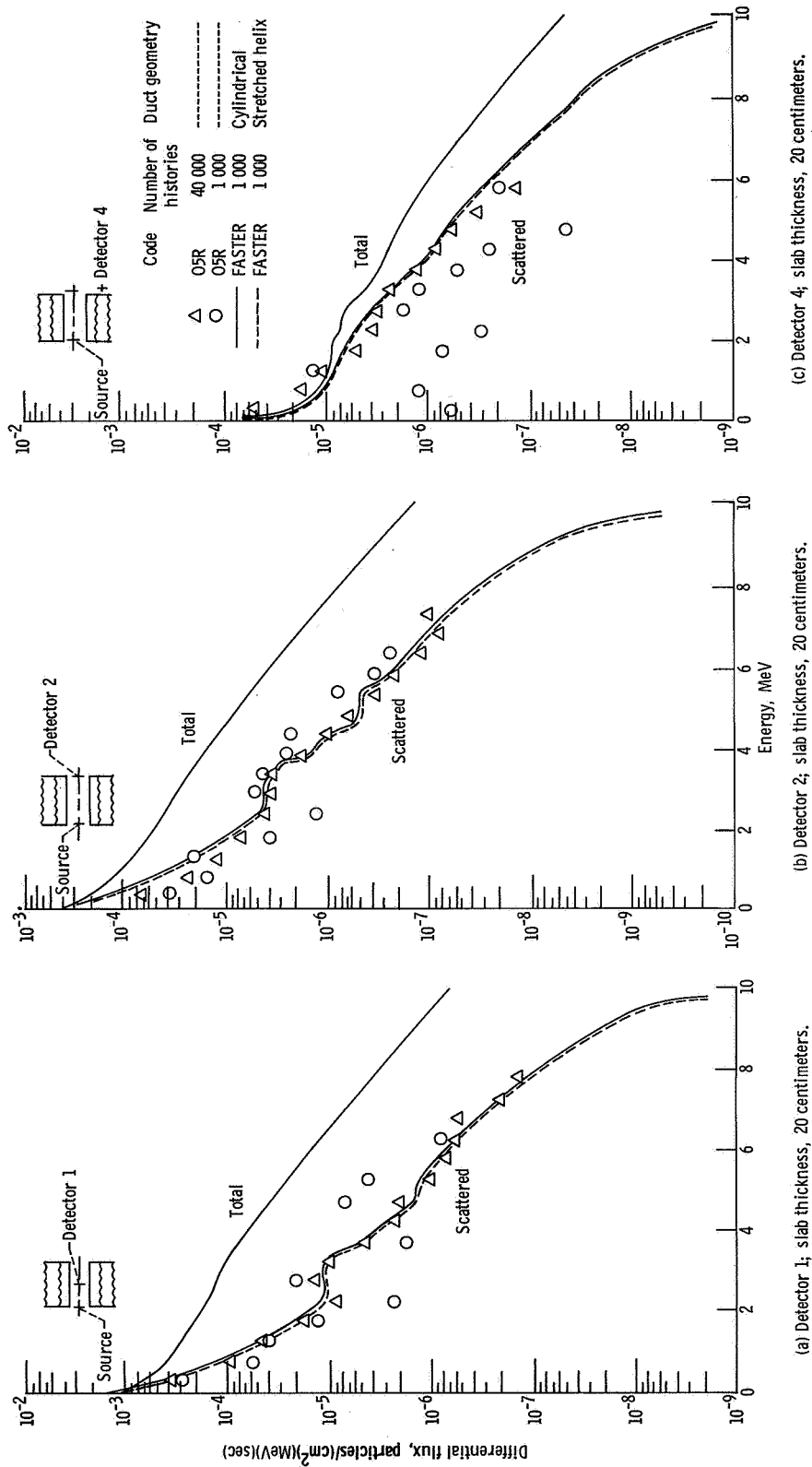


Figure 2. - Differential flux as function of energy.

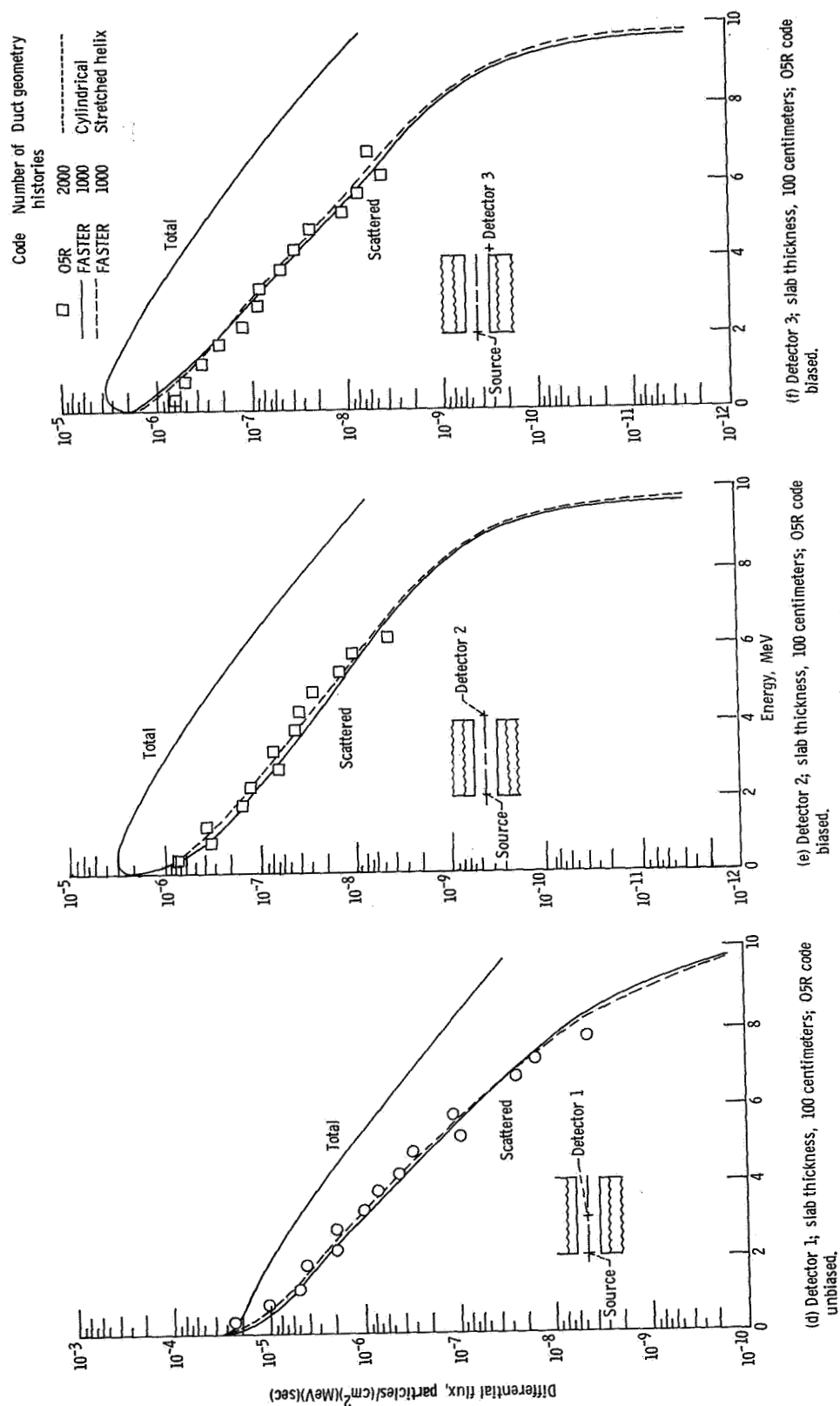


Figure 2. - Concluded.

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